Health versus Wealth: On the Distributional Effects of Controlling a Pandemic

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April 18, 2020
First version, March 31 2020

Abstract

To slow the spread of COVID-19, many countries are shutting down non-essential sectors of the economy. Older individuals have the most to gain from slowing virus diffusion. Younger workers in sectors that are shuttered have the most to lose. In this paper, we build a model in which economic activity and disease progression are jointly determined. Individuals differ by age (young and retired), by sector (basic and luxury), and by health status. Disease transmission occurs in the workplace, in consumption activities, at home, and in hospitals. We study the optimal economic mitigation policy of a utilitarian government that can redistribute across individuals, but where such redistribution is costly. We show that optimal redistribution and mitigation policies interact, and reflect a compromise between the strongly diverging preferred policy paths of different subgroups of the population. We find that the shutdown in place on April 12 is too extensive, but that a partial shutdown should remain in place through July.

Keywords: COVID-19; Economic Policy; Redistribution

*We thank Josep Pijoan-Mas, Marc Suchard, and Andrew Atkeson for helpful comments. We thank attendees at virtual talks at the Minneapolis Fed, the VMACS seminar series, and the Bank of England. The views expressed herein are those of the authors and not necessarily those of the Federal Reserve banks of Kansas City and Minneapolis or the Federal Reserve System.

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1 Introduction

The central debate about the appropriate economic policy response to the global COVID-19 pandemic is about how aggressively to restrict economic activity in order to slow down the spread of the virus and how quickly to lift these restrictions as the pandemic shows signs of subsiding. In this paper, we argue that one reason people disagree about the appropriate policy is that “lock-down” policies have very large distributional implications. These distributional effects mean that different groups prefer very different policies. Standard epidemiological models assume a representative agent structure, in which households face a common trade-off between restrictions on social interaction that slow the virus transmission but which also depress economic activity. In practice, however, the benefits of slower viral transmission are not shared uniformly but accrue disproportionately to older households, which face a much higher risk of serious illness or death from infection. At the same time, the costs of reduced economic activity are disproportionately borne by younger households, which bear the brunt of lower employment. A second very important dimension of heterogeneity is among younger workers employed in different sectors of the economy. Sensible lock-down policies designed to reduce viral spread will naturally focus on reducing activity in sectors in which there is a social aspect to consumption and sectors that produce goods or services perceived to be luxuries. For example, restaurants and bars are likely to be close first. Because workers cannot easily reallocate across sectors, this implies that lock-down policies will involve extensive redistribution among young households specialized in different sectors. Thus, different groups in the economy (old versus young, workers in different sectors, healthy versus sick) will likely have very different views about the optimal mitigation strategy. Furthermore, lock-down policies create a need for potentially large redistributive public policies. To the extent that these are costly to implement, the optimal mitigation policy will in turn depend on the scope for redistributive policies at the micro level.

In this paper, we build and then quantitatively implement a model that implements this interaction between macro-mitigation and micro-redistribution policies. This requires a structure with (i) a household sector with heterogeneous individuals, (ii) an epidemiological block where consumption, production, caring for the sick and purely social interactions determine health transitions during the epidemic, and (iii) a government with tools for mitigation and redistribution, as well as a desire for social insurance.

On the household side, we distinguish between three types of people: young workers in a basic sector, young workers in a luxury sector, and old retired people. The output of workers in
the two sectors is combined to produce a single final consumption good. Workers are immobile across sectors. The output of the basic sector is assumed to be so essential that it will not make sense to reduce employment and output in that sector in order to reduce the spread of the disease. In contrast, the policy maker has a potential incentive to shut down part of the economic activity in the luxury sector in order to reduce the rate at which infection spreads.

The epidemiological structure builds on a standard Susceptible-Infectious-Recovered (SIR) diffusion framework. We label our variant a SAFER model, reflecting the progression of individuals through a sequence of possible health states. Model individuals start out as susceptible, S (i.e., healthy, but vulnerable to infection), and can then become infected but asymptomatic, A; infected with flu-like symptoms, F; infected and needing emergency hospital care, E; recovered, R (healthy and immune), or dead. The transition rates between these states vary with age. In particular, the old are much more likely to experience adverse health outcomes conditional on being infected.

At the heart of the model are a range of two-way interactions between the distributions of health and economic activity. We model virus transmission from co-workers in the workplace, from co-consumers in the marketplace, from friends and family at home, and from the sick in hospitals. Because they do not work, the old do not face direct exposure at work, but virus transmission in the workplace indirectly increases infection rates in other settings. Our three different infected subgroups spread the virus in different ways: the asymptomatic are unlikely to realize they are contagious and will continue to work and to consume; those with flu symptoms will stay at home and only infect family members, while those in hospital care may pass the virus to health care workers.

The government uses a utilitarian social welfare function and has at its disposal two policy levers to maximize social welfare. First, at each date, the planner can choose what fraction of activity in the luxury sector to shut down. We call this policy the extent of mitigation. Mitigation slows the spread of the virus (by reducing the rate at which susceptible workers become asymptotically infected), but it reduces to zero the market income of some workers in the luxury sector. Second, the planner chooses how much income to redistribute from those working toward those that are not, because they are old, because they are unwell, or because their workplaces have been closed owing to mitigation. Redistribution is desirable because of the utilitarian social welfare function, but crucially, we also assume that this redistribution is costly, so that perfect insurance is not optimal. Conditional on a given path for mitigation, the optimal
redistribution problem is equivalent to a static social planner problem, with lower aggregate consumption and more consumption inequality across workers as is redistribution becomes more costly. This in turn feeds back adversely on the dynamic incentives for mitigation, implying that a government facing more costly redistribution needs will dynamically choose less mitigation.

In the context of the model with these trade-offs, we then compute optimal paths for mitigation, where the path for mitigation is restricted to a simple parametric function of time. We find that a planner who prioritizes the old chooses extensive and prolonged mitigation, as the old are highly vulnerable to contracting and dying from the disease. A planner who prioritizes workers in the luxury sector subject to shut-downs chooses a much milder and shorter mitigation path, as the economic costs of forgone income and thus consumption dominate for this group.

We also consider how the optimal policy for a utilitarian equal-weights planner varies with the cost of redistribution across worker types. We find that the larger this cost is, the more moderate is optimal mitigation, at the cost of higher mortality during the epidemic.

Under our baseline calibration, a comparison of the utilitarian optimal policy to the actual policy in place as of April 12 indicates that the shutdown in place is around twice as extensive as it should be. However, the optimal policy calls for leaving a partial shutdown in place through July. Ending the shutdown at Easter would have implied an additional 172,000 deaths.

There is an extraordinary set of papers currently being written about the pandemic. To cite the ones that we are aware of: Atkeson (2020) was perhaps the first to introduce economists to the epidemiological SIR class of models. He emphasizes the negative outcomes that arise if and when the fraction of active infections in the population exceeds 1% (at which point the health system is predicted to be severely challenged) and 10% (which may result in severe staffing shortages in key financial and economic infrastructure sectors) as well as the cumulative burden of the disease over an 18-month horizon. Greenstone and Nigam (2020) use the state-of-the-art Imperial College epidemiological model (Flaxman et al. 2020) to compare the paths under moderate social distancing versus no policy action and use the statistical value-of-life approach to assess the social cost of no action. They calculate 1.7 million lives saved between March 1 and October 1 from social distancing, 37% of them due to less overcrowding in hospitals.

Eichenbaum et al. (2020) extend the canonical SIR epidemiology model to study the interaction between economic decisions and pandemics. They emphasize how equilibria without interventions lead to sub-optimally severe pandemics, because infected people do not fully in-
ternalize the effects of their economic decisions on the spread of the virus. Krueger et al. (2020) argue that the severity of the economic crisis in Eichenbaum et al. (2020) is much smaller if individuals can endogenously adjust the sectors in which they consume. Toxvaerd (2020) characterizes the simultaneous determination of infection and social distancing. Moll et al. (2020) develop a version of a HANK model, in which agents differ by occupation and occupations have two key characteristics: how social their consumption is, and how easily work in the occupation can be done at home. They tie demand for social goods and willingness to work in the workplace to fear of contracting the virus, with endogenous feedback to relative earnings by occupation. Bayer and Kuhn (2020) explore how differences in living arrangements of generations within families contribute to the cross-country differences in terms of case-fatality rates. They document a strong positive correlation between this variable and the share of working-age families living with their parents. Berger et al. (2020) extend the baseline Susceptible-Exposed-Infectious-Recovered (SEIR) infectious-disease model to explore the role of testing and to thereby get a better idea of how to implement selective social separation policies. Using the Chinese experience, Fang et al. (2020) quantify the causal impact of human mobility restrictions and find that the lock-down was very effective, providing estimates of diffusion under different scenarios. Hall et al. (2020) provide a simple calculation to assess how much people would be willing to pay to have never had the virus (their answer is about a quarter of one year’s worth of consumption).

In Section 2, we start by describing how we model the joint evolution of the economy and the population. In Section 3, we then turn to describe how we model mitigation and redistribution policies and how we go about solving for optimal policies. The calibration strategy is described in Section 4. The findings are in Section 5.

2 The Model

We first describe the individual state space, describing the nature of heterogeneity by age and health status. In Section 2.2, we then describe the multi-sector production technology, describing how mitigation shapes the pattern of production. Section 2.3 describes the details of our SAFER extension of the standard SIR epidemiological model and the channels of disease transmission.
2.1 Household Heterogeneity

Agents can be young or old, which we denote $y$ and $o$, respectively. We think of the young as below the age of 65 and they will comprise $\mu_y = 85$ percent of the population. For simplicity, and given the short time horizon of interest, we abstract from population growth and ignore aging.

Within each age group, agents are differentiated by health status, which can take six different values: susceptible $s$, asymptomatic $a$, miserable with flu symptoms $f$, requiring emergency care $e$, recovered $r$, or dead $d$. Individuals in the first group have no immunity and are susceptible to infection. The $a$, $f$, and $e$ groups all carry the virus – they are subsets of the infected group in the standard $SIR$ model – and can pass it onto others. However, they differ in their symptoms. The asymptomatic have no symptoms or very mild ones and thus unknowingly spread the virus. We model this state explicitly (in contrast to the prototypical $SIR$ model) because a significant percentage of individuals infected with COVID-19 experience no symptoms.\(^1\) Those with flu-like symptoms are sufficiently sick to know they are likely contagious, and they stay at home and avoid the workplace and market consumption. Those requiring emergency care are hospitalized. The recovered are again healthy, no longer contagious, and immune from future infection. A worst-case virus progression is from susceptible to asymptomatic to flu to emergency care to dead.\(^2\) However, recovery is possible from the asymptomatic, flu, and emergency-care states.

2.2 Activity: Technology and Mitigation

Young agents in the model are further differentiated by the sector in which they can work. A fraction $\mu_b$ of the young work in the basic sector, denoted $b$, while the rest, $1 - \mu_b$, work in a luxury sector, denoted $\ell$. We assume that output of the basic sector is so vital that it is never optimal to send home even a subset of $b$ sector workers. In contrast, it may be optimal to require some or all of the workers in the $\ell$ sector to stay at home in order to reduce the transmission of the virus in the workplace. We will call such a policy a (macroeconomic)\(^1\) deCODE, a subsidiary of Amgen, randomly tested 9,000 individuals in Iceland. Of the tests that came back positive (1 percent), half reported experiencing no symptoms.\(^2\) Note that in the standard SEIR model, agents in the exposed state $E$ have been exposed to the virus and may fall ill, but until they enter the infected state $I$, they cannot pass the virus on. Our asymptomatic state is a hybrid of the $E$ and the $I$ states in the SEIR model: asymptomatic agents have no symptoms (as in the SEIR $E$ state) but can pass the virus on (as in the SEIR $I$ state). Berger et al. (2020) make a similar modeling choice.
mitigation policy, \( m \). More precisely, \( m_t \) will denote the fraction of luxury workers that are instructed to not go to work at time \( t \). We assume that workers cannot change sectors (at least, not during the short time horizon studied in this paper); thus, the sector of work is a fixed characteristic of a young individual.

Time starts at \( t = t_0 \) and evolves continuously. All economic variables, represented by roman letters, are understood to be functions of time, but we suppress that dependence whenever there is no scope for confusion. Technology parameters are denoted with Greek letters. Generically, we use the letter \( x \) to denote population measures, with superscripts specifying subsets of the population. These super-indices index age, sector, and health status, in that order. For example, \( x^{ybs} \) is the measure of young individuals working in the basic sector who are susceptible.

We assume a production technology that is linear in labor, and thus output in the basic sector is given by the number of young workers employed there:

\[
y^b = x^{ybs} + x^{yba} + x^{ybr}.
\]

(1)

Note that this specification assumes that those asymptomatic individuals carrying the virus continue to work.\(^3\) In contrast, we assume those with flu stay at home. Output in the luxury sector, in contrast, does depend on the mitigation policy and is given by

\[
y^\ell = (1 - m_t) \left( x^{y\ell s} + x^{y\ell a} + x^{y\ell r} \right).
\]

(2)

We assume that both sectors produce the same good and are perfect substitutes.\(^4\) Under this assumption, total output of the single consumption good is determined by

\[
y = y^b + y^\ell.
\]

(3)

We assume that a fixed amount of output \( \eta \Theta \) is spent on emergency hospital care, where \( \Theta \) is the capacity of hospital beds, and \( \eta \) is the cost of providing and maintaining one bed.

In practice, different sectors of the economy are heterogeneous with respect to the extent to which production and consumption generate risky social interaction. For example, some

\(^3\)One could instead imagine a policy of tracing contacts of infected people, which would allow the planner to keep some portion of exposed workers at home.

\(^4\)We make this assumption primarily for the sake of tractability. If outputs of the two sectors were complementary, there would be changes in relative prices and wages when output of the luxury sector was suppressed.
types of work and market consumption can easily be done at home, while for others, avoiding interaction is much harder. A sensible shutdown policy will first shutter those sub-sectors of the luxury sector that generate the most interaction. Absent detailed micro data on social interaction by sector, we model this in the following simple way.\(^5\) Assume workers are assigned to a unit interval of sub-sectors \(i \in [0, 1]\) where sub-sectors are ranked from those generating the least to those generating the most social interaction.

Assume the sector-specific infection-generating rates are \(\beta_w^i = 2\alpha_w i\) and \(\beta_c^i = 2\alpha_c i\), where \((\alpha_w, \alpha_c)\) are parameters, to be calibrated below, governing the intensity by which meetings among individuals generate infections. When the government asks fraction \(m_t\) of luxury workers to stay at home, assume it targets the sub-sectors generating the most interactions, that is, \(i \in [1 - m_t, 1]\). The average interaction rates of the sectors that remain are then \(\alpha_w(1 - m_t)\) and \(\alpha_c(1 - m_t)\), respectively\(^6\). Because the government cannot shut down any basic sub-sectors of the economy, the economy-wide work-related infection-generating probability is then given by

\[
\beta_w(m_t) = \frac{y_b}{y(m_t)} \alpha_w + \frac{y'(m_t)}{y(m_t)} \alpha_w(1 - m_t),
\]

with an analogous expression for \(\beta_c(m_t)\). The key property of this expression is that as mitigation is increased, the average social interaction-generating rate will fall.

2.3 Health Transitions: The SAFER Model

We now describe the dynamics of individuals across health states. At \(t_0\), the total mass of individuals is one, \(x^{yb} + x^{y\ell} + x^o = 1\), where \(x^{yb} = \sum_{i \in \{s, a, f, e, r\}} x^{ybi}\), \(x^{y\ell} = \sum_{i \in \{s, a, f, e, r\}} x^{y\ell i}\), and \(x^o = \sum_{i \in \{s, a, f, e, r\}} x^{oi}\). In the interest of more compact notation, we will also let \(x^i = x^{ybi} + x^{y\ell i} + x^{oi}\) for \(i \in \{s, a, f, e, r\}\) denote the total number of individuals in health state \(i\). Finally, at any point in time, let \(x = \sum_{i \in \{s, a, f, e, r\}} x^i = x^{yb} + x^{y\ell} + x^o\) denote the entire living population.

The crucial health transitions that can, in our model, be affected by mitigation policies are from the susceptible to the asymptomatic state. These are characterized by equations (4)-(9) below. Equations (4)-(6) capture the flow of basic sector workers, luxury sector workers, and older individuals out of the susceptible state and into the asymptomatic state. The number of

\(^5\)See Xu et al. (2020) for more detailed evidence on infection patterns in the workplace.

\(^6\)\(E[\alpha_w i | i \leq (1 - m_t)] = \frac{2\alpha_w}{1 - m_t} \int_0^{1 - m_t} i di = \frac{2\alpha_w}{1 - m_t} \frac{(1 - m_t)^2}{2} = \alpha_w(1 - m_t)\).
such workers who catch the virus is their original mass ($x^{ybs}$ for young basic sector workers, for example) times the number of virus-transmitting interactions they have (the term in square brackets). We model four sources of possible virus contagion: people can catch the virus from colleagues at work, from market consumption activities, from family or friends outside work, and from taking care of the sick in hospitals. The four terms in the bracket capture these four sources of infection, which we index $w, c, h, e$, respectively. For a given type of individual, the flow of new infections from each of these activities is the product of the number of contagious people they can expect to meet, which we denote $\mu_j(m_t)$ for $j \in \{w, c, h, e\}$, and the likelihood that such meetings result in infection, which is the infection-generating rate described above, $\beta_j(m_t)$. For work and consumption activities, both the number of contagious people in a given setting and the rate at which they transmit the virus potentially depend on the level of economic mitigation $m_t$. 

$$\dot{x}^{ybs} = -[\beta_w(m_t)\mu_w(m_t) + \beta_c(m_t)\mu_c(m_t) + \beta_h\mu_h + \beta_e\mu_e] x^{ybs} \quad (4)$$
$$\dot{x}^{\ell a} = -[\beta_w(m_t)\mu_w(m_t)(1 - m_t) + \beta_c(m_t)\mu_c(m_t) + \beta_h\mu_h] x^{\ell a} \quad (5)$$
$$\dot{x}^{os} = -[\beta_c(m_t)\mu_c(m_t) + \beta_h\mu_h] x^{os} \quad (6)$$

where the relevant population shares $\mu$ in the above expressions are given by

$$\mu_w(m_t) = x^{yba} + (1 - m_t)x^{\ell a} \quad (7)$$
$$\mu_c(m_t) = x^\ell y(m_t) \quad (8)$$
$$\mu_h = x^\ell + x^e \quad (9)$$
$$\mu_e = x^e \quad (10)$$

Consider the first outflow rate in equation (4). The flow of young basic sector workers getting infected at work, $\beta_w(m_t)\mu_w(m_t)$, is the probability of a virus-spreading interaction per contagious worker, $\beta_w(m_t)$, times the number of contagious workers, which is defined in equation (7). Note that we are assuming that people with symptoms always stay at home (a minimal precaution) and that basic and luxury workers mingle together at work.

The flow of young basic sector workers getting infected from market consumption, $\beta_c(m_t)\mu_c(m_t)$, is similarly constructed. We assume that the number of consumption-related infections is pro-
portional to the number of asymptomatic individuals in the population and to the level of economic activity, which is identical to the number of workers (see equation 8).\footnote{Note that we have assumed that the number of shopping-related infections for a given type is proportional to economy-wide output, rather than to the type-specific level of consumption. One interpretation of this assumption is that each consumer visits each store in the economy and faces a similar infection risk irrespective of how much they spend. The common infection risk is proportional to the equilibrium number of stores, which in turn is proportional to the aggregate employment level.} Note that we are assuming that people with symptoms stay at home and do not go shopping.

The rate at which a young basic worker contracts the virus at home, $\beta_h \mu_h$, depends on the number of contagious workers in the household, $\mu_h$ defined in equation (9). Note that both asymptomatic and flu-suffering workers reside at home. Finally, we assume that caring for those requiring emergency care is a task that falls entirely on basic workers. The risk of contracting the virus from this activity is proportional to the number of hospitalized people, $\mu_e = x^e$, with infection-generating rate $\beta_e$, which reflects the strength of precautions taken in hospitals.

Parallel to equation (4), equation (5) describes infections for the susceptible population working in the luxury sector. For this group, the risks of infection from market consumption and at home are identical to those for basic sector workers. However, individuals in this sector work reduced hours when $m_t > 0$ and thus have fewer work interactions in which they could get infected. Furthermore, workers in the luxury sector do not take care of sick patients in hospitals, and thus the last term in equation (4) is absent in equation (5). Similar to equation (4) and equation (5), equation (6) displays infections among the old. They get infected only from market consumption and from interactions at home.

The remainder of the epidemiological block is fairly mechanical and simply describes the transition of individuals through the health states (asymptomatic, flu-suffering, hospitalized, and recovered) once they have been infected. The parameters of these dynamic laws in equation (11) to equation (22) are allowed to vary by age. Equations (11) to (13) describe the change in the measure of asymptomatic individuals. There is entry into that state from the newly infected flowing in from the susceptible state (as described above). Exit from this state to developing flu-like symptoms occurs at rate $\sigma_{yaf} (\sigma_{oaf})$ for the young (old), and exit to the recovered state occurs at rate $\sigma_{yar} (\sigma_{oar})$ for the young (old). Note that someone who recovers at this stage will never know that she contracted the virus.

For individuals suffering from the flu, equations (14) to (16) show that for the young there is entry from the asymptomatic state and exit to the hospitalized state at rate $\sigma_{yfe}$, and to the
recovered state at rate $\sigma^{yfr}$, with analogous expressions for the old. Equations (17) to (19) describe the movements of those in emergency care, showing entry from those with flu-like symptoms and exits to death and recovery. The death rate is $\sigma^{yed} + \varphi$, while the recovery rate is $\sigma^{yer} - \varphi$, where $\varphi$, described below, is a term related to hospital overuse. Equations (20) to (22) display the evolution of the measure of the recovered population, which features only entry and is an absorbing state. So is death, with the evolution of the deceased population being determined by $\dot{Y}_{bd} = (\sigma^{yed} + \varphi) Y_{be}$, $\dot{Y}_{ld} = (\sigma^{yed} + \varphi) Y_{le}$, and $\dot{Y}_{od} = (\sigma^{oed} + \varphi) Y_{oe}$. We record them separately from the recovered (who work), since they play no further role in the model.

Finally, equation (23) describes the extent of overuse of the hospital system that has capacity $\Theta$, which we treat as fixed in the time horizon analyzed in this paper. The probability of death conditional on being sick depends on the extent of hospital overuse. In particular, the parameter $\lambda_o$ controls how much the death rate of the hospitalized rises (and the recovery rate falls) once hospital capacity $\Theta$ is exceeded.

\[
\begin{align*}
\dot{Y}_{ba} &= -\dot{Y}_{bs} - (\sigma^{yaf} + \sigma^{yfr}) Y_{ba} \\
\dot{Y}_{a} &= -\dot{Y}_{as} - (\sigma^{oaf} + \sigma^{oar}) Y_{a} \\
\dot{Y}_{bf} &= \sigma^{yaf} Y_{ba} - (\sigma^{yfe} + \sigma^{yfr}) Y_{bf} \\
\dot{Y}_{lf} &= \sigma^{yaf} Y_{la} - (\sigma^{yfe} + \sigma^{yfr}) Y_{lf} \\
\dot{Y}_{of} &= \sigma^{oaf} Y_{oa} - (\sigma^{oef} + \sigma^{oer}) Y_{of} \\
\dot{Y}_{be} &= \sigma^{yfe} Y_{bf} - (\sigma^{yed} + \sigma^{yer}) Y_{be} \\
\dot{Y}_{le} &= \sigma^{yfe} Y_{lf} - (\sigma^{yed} + \sigma^{yer}) Y_{le} \\
\dot{Y}_{o} &= \sigma^{oef} Y_{of} - (\sigma^{oed} + \sigma^{oer}) Y_{o} \\
\dot{Y}_{br} &= \sigma^{yar} Y_{ba} + \sigma^{yfr} Y_{bf} + (\sigma^{yer} - \varphi) Y_{be} \\
\dot{Y}_{lr} &= \sigma^{yar} Y_{la} + \sigma^{yfr} Y_{lf} + (\sigma^{yer} - \varphi) Y_{le} \\
\dot{Y}_{or} &= \sigma^{oar} Y_{oa} + \sigma^{ofr} Y_{of} + (\sigma^{oer} - \varphi) Y_{oe}
\end{align*}
\]
\[ \varphi = \lambda_o \max\{x^e - \Theta, 0\}. \quad (23) \]

### 2.4 Preferences

Preferences incorporate utility from both being alive and being in a specific health state. Lifetime utility for the old is given by

\[ E \left\{ \int e^{-\rho_o t} \left[ u(c^o_t) + \bar{u} + \tilde{u}_t^j \right] \, dt \right\}, \quad (24) \]

where expectations are taken with respect to the random timing of death, and where \( \bar{u} \) measures the flow utility from being alive (the utility of being dead is implicitly zero). Similarly, \( \tilde{u}_t^j \) is the intrinsic utility of being in state health \( j \). We will assume that \( \bar{u}_t^o = \bar{u}_t^a = \bar{u}_t^r = 0 \), while \( \bar{u}_t^e < \bar{u}_t^r < 0 \). Thus, having flu-like symptoms is bad, and having to be treated in the hospital is very bad. The old value their consumption \( c^o_t \) according to the period utility function \( u(c^o_t) \) and discount the future at rate \( \rho_o \).

Symmetrically, the young also care about their consumption \( c^y_t \), as well as about their health and about being alive, according to the lifetime utility function:

\[ E \left\{ \int e^{-\rho_y t} \left[ u(c^y_t) + \bar{u} + \tilde{u}_t^j \right] \, dt \right\}. \quad (25) \]

In our calibration, we will impose \( \rho_o > \rho_y \) as a simple way to capture higher life expectancy for the young. As a result, while young and old enjoy the same flow value from being alive, the present value of this value will be lower for the old.

Note that workers who experience flu-like symptoms or are in the hospital do not work. Neither does a fraction \( m \) of luxury sector workers whose workplaces have been shut down by mitigation policy. Therefore, in equilibrium, young workers will experience different consumption depending on whether they work. Thus, the expected utility of a worker will depend for two reasons on the sector in which she works. First, sectors differ in the share of economic activity being shut down (and thus, for the individual worker, in the probability of being able to work when healthy). Second, a worker’s sector will affect her distribution of health outcomes.\(^8\)

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\(^8\)Note that we have not modeled mortality from natural causes. Over the expected length of the COVID-19 pandemic, mortality from natural causes will be small for both age groups.
3 The Public Sector

In Section 3.1 we describe the government policy tools, and then in Section 3.2, we analyze how public transfers are determined statically to yield a utilitarian period social welfare function. We conclude by posing the dynamic Ramsey optimal policy problem, which maximizes the time integral of discounted instantaneous social welfare by choice of the optimal time path of mitigation $m_t$.

3.1 Transfers

The public sector is responsible for two choices: mitigation (shutdowns) $m_t$ and redistribution from workers to individuals who do not or cannot work: those unemployed because of shutdowns, those with flu or hospitalized, and those who have retired. All workers share a common consumption level $c_w$ and all individuals not working share a common consumption level $c_n$.

The redistribution policy choice is how much to transfer, in each instant $t$, from the working to the non-working population. Crucially, we assume that these transfers are costly, denoting by $T(c_n)$ the per capita cost of transferring consumption $c_n$ to those out of work and without current income. We assume that $T(.)$ is increasing and differentiable.

To simplify notation, denote by $(\mu^n(m, x), \mu^w(m, x))$ the mass of non-working and working people, respectively, as a function of the health population distribution $x$ and current mitigation $m = m_t$. These are defined as

\[
\mu^n(m, x) = x^y \ell^f + x^y \ell^e + x^y b^f + x^y b^e + m \left( x^y \ell^s + x^y \ell^a + x^y \ell^r \right) + x^o \tag{26}
\]

\[
\mu^w(m, x) = x^y b^s + x^y b^a + x^y b^r + [1 - m] \left( x^y \ell^s + x^y \ell^a + x^y \ell^r \right) \tag{27}
\]

\[
\nu^w(m, x) = \frac{\mu^w(m, x)}{\mu^w(m, x) + \mu^n(m, x)}, \tag{28}
\]

where $\nu^w(m, x)$ is the share of working individuals in the population. The aggregate resource

\[\text{\footnotesize{\textsuperscript{9}}This is the allocation chosen by a government that equally values all individuals (equal Pareto weights). It is also the only allocation that is feasible if the government can observe an individual's income but not her sector, age, or health status.}

\[\text{\footnotesize{\textsuperscript{10}}We will suppress the dependence on $(x, m)$ when there is no room for confusion.}}\]
constraint can then be written as

\[ \mu^w c^w + \mu^n c^n + \mu^n T(c^n) = y - \eta \Theta = \mu^w - \eta \Theta \quad (29) \]

where \( y = \mu^w \) since each working individual produces one unit of output.

Notice that there are no dynamic consequences of the transfer choice \( c^n \). In particular, this choice has no impact on any health transitions. At each date \( t \), we can therefore solve a static optimal transfer problem (given the current level of mitigation \( m = m_t \)) that delivers a maximum level of instantaneous social welfare which we denote \( W(m, x) \). We turn to derive this expression now.

### 3.2 The Instantaneous Social Welfare Function

We now derive the instantaneous social welfare function \( W(x, m) \), a necessary ingredient for the optimal mitigation problem of the government. Assuming that all individuals have log-utility and receive the same social welfare weights, the function \( W(x, m) \), is given by

\[ W(x, m) = \max_{c^n, c^w} \left[ \mu^w \log(c^w) + \mu^n \log(c^n) \right] + (\mu^w + \mu^n) \bar{u} + \sum_{ij} x_{ij} \hat{u}_j, \quad (30) \]

where the maximization is subject to the aggregate resource constraint (29). Combining the first order conditions with respect to \((c^n, c^w)\) yields

\[ \frac{c^w}{c^n} = 1 + T'(c^n). \quad (31) \]

We can use this relation in the resource constraint to obtain

\[ \mu^w (1 + T'(c^n)) c^n + \mu^n c^n + \mu^n T(c^n) = \mu^w - \eta \Theta. \quad (32) \]

Defining net per-capita income \( \tilde{y} \) and average transfer costs \( t(c^n) \) as

\[ \tilde{y} = \nu - \frac{\eta \Theta}{\mu^w + \mu^n}, \quad (33) \]
\[ t(c^n) = \frac{T(c^n)}{c^n}. \quad (34) \]
we can rewrite the resource constraint in per-capita terms by dividing by $\mu^w + \mu^n$

$$c^n [1 + \nu T'(c^n) + (1 - \nu)t(c^n)] = \bar{y}.$$  \hspace{1cm} (35)

Thus, the optimal solution to the government transfer problem is given by the solution to the following system:

$$c^n [1 + \nu T'(c^n) + (1 - \nu)t(c^n)] = \bar{y} \hspace{1cm} (36)$$

$$c^w = c^n(1 + T'(c^n))) \hspace{1cm} (37)$$

for an arbitrary differentiable per capita transfer cost function $T(.)$. We can also express period welfare in per capita terms, using

$$W(x, m) = [\mu^w + \mu^n] w(x, m) \hspace{1cm} (38)$$

$$w(x, m) = \log(c^n) + \nu \log(1 + T'(c^n)) + \bar{u} + \sum_{i,j} \frac{x^{ij}}{\mu^w + \mu^n \tilde{u}^j}, \hspace{1cm} (39)$$

where the only endogenous input in the period welfare function $c^n$ solves equation (36). In particular, note that $\mu^w + \mu^n$ is independent of mitigation, and thus we can discuss the impact of mitigation on current welfare in terms of the per capita welfare function $w(x, m)$.

The per capita welfare function illustrates the basic costs from mitigation $m$. First, mitigation lowers per capita income and, through it, the level of consumption. This is the $\log(c^n)$ term in $w(x, )$ which is strictly increasing in net income $\bar{y}$. In the absence of the cost of transfers, this is the only direct effect of current mitigation. Second, the transfer cost to non-working households distorts risk sharing; this is the second term $\nu \log(1 + T'(c^n))$, which is zero if the marginal transfer cost is zero. Note that an increase in mitigation reduces $\nu$, and thus the greater the severity of the negative impact of mitigation on current welfare, the larger the marginal cost of transfers is. This, ceteris paribus, will reduce the incentives of the government to engage in economically costly mitigation.

To see most clearly the intuition for our results, assume that the transfer cost is linear such that $T(c^n) = \tau c^n$. In this case the optimal allocation is given by

$$c^w = \bar{y}$$

15
\[
\begin{align*}
    c^n &= \frac{\tilde{y}}{1 + \tau} \\
    w(x, m) &= \log(\tilde{y}) - (1 - \nu) \log(1 + \tau) + \bar{u} + \sum_{ij} x_{ij} \mu_i + \mu_j \bar{w}_{ij}.
\end{align*}
\]

Thus, the negative economic impact of mitigation is given, in this case, by
\[
\frac{\partial w(x, m)}{\partial m} = \frac{\partial \tilde{y}}{\partial m} + (1 + \tau) \frac{\partial \nu}{\partial m} < 0, \quad (40)
\]

since both \(\frac{\partial \tilde{y}}{\partial m}\) and \(\frac{\partial \nu}{\partial m}\) are negative. In addition, we observe that the larger the marginal cost of transfers \(\tau\), the more negative \((1 + \tau)\frac{\partial \nu}{\partial m}\) is. This is how mitigation and redistribution costs interact: the larger the marginal cost of redistribution is, the larger the economic cost of mitigation \(\frac{\partial w(x, m)}{\partial m}\) is.

In our quantitative exercises, we will assume that the transfer cost function per non-worker is given by the quadratic form
\[
T(c^n) = \frac{\tau}{2} \left( \frac{\mu^n c^n}{\mu^n} \right)^2 = \frac{\tau}{2} \left( \frac{1 - \nu}{\nu} \right) (c^n)^2
\]
so that total transfer costs are given by \(\mu^n T(c^n) = \mu w \frac{\tau}{2} \left( \frac{\mu^n c^n}{\mu^n} \right)^2\). This functional form is motivated by the idea that each working household has to transfer \(\left( \frac{\mu^n c^n}{\mu^n} \right)\) units of consumption to non-working households. Assuming a quadratic cost of extracting resources from workers, the per-worker cost is thus given by \(\frac{\tau}{2} \left( \frac{\mu^n c^n}{\mu^n} \right)^2\). Multiplying this by the total number of workers \(\mu^w\) gives the total transfer cost.\(^{11}\) For this specification, we obtain as optimal allocations to be inserted in the period welfare function above
\[
\begin{align*}
    c^n &= \frac{\sqrt{1 + 2 \tau \frac{1 - \nu}{\nu} \tilde{y} - 1}}{\tau \frac{1 - \nu^2}{\nu}} \quad (41) \\
    c^w &= c^n(1 + T'(c^n)) = c^n \left( 1 + \tau \frac{1 - \nu}{\nu} c^n \right). \quad (42)
\end{align*}
\]

Note that \(\left( 1 + \tau \frac{1 - \nu}{\nu} c^n \right)\) is the effective price the planner has to pay on the margin to take one more unit of output from workers to give to non-workers. As transfers and thus non-worker consumption \(c^n\) rise, this price effectively rises, reflecting a higher marginal cost to additional redistribution. In addition, since higher mitigation \(m\) reduces the share of workers \(\nu\) and increases the share of non-workers \(1 - \nu\), the effective price of transfers at the margin \(\]

\(^{11}\) The quadratic form is chosen for analytical convenience but is not central for our qualitative arguments.
increases with mitigation, and the price rises the higher $\tau$ is.

For future reference, we can also construct expected flow utility for each type

$$W^\ell(x, m) = \frac{(x^{y\ell n} + x^{y\ell e} + x^{y\ell r})}{x^\ell} [(1 - m)u(c^w) + mu(c^n) + \bar{u}] + \frac{(x^{y\ell f} + x^{y\ell e})}{x^\ell} [u(c^n) + \bar{u} - \hat{u}]$$

$$W^b(x, m) = \frac{(x^{ybn} + x^{ybe} + x^{ybr})}{x^b} [u(c^w) + \bar{u}] + \frac{(x^{ybf} + x^{ybe})}{x^b} [u(c^n) + \bar{u} - \hat{u}]$$

$$W^o(x, m) = u(c^n) + \bar{u} - \frac{(x^{yof} + x^{yoe})}{x^o} \hat{u}.$$

### 3.3 Optimal Policy

We now assume there is a government/planner (we use these names synonymously, as there is no time consistency problem) that chooses optimal policy over time by choosing the path of mitigation $m(t)$; the optimal choice of redistribution $T(t)$ is already embodied in the period social welfare function $W(x)$. The policy problem the planner solves is then given by

$$\max_{m(t)} \int_0^\infty e^{-\rho t} W(x) \, dt,$$

subject to the laws of motion of the population equation (4) to equation (23).

In a first step, we will approximate the optimal time path of mitigation by functions that are part of the following parametric class of generalized logistic functions of time:

$$m(t) = \frac{\gamma_0}{1 + \exp(-\gamma_1(t - \gamma_2))}.$$  

Here, the parameter $\gamma_0$ controls the level of mitigation at $t = 0$. The parameter $\gamma_2$ governs when mitigation is reduced, and the parameter $\gamma_1$ commands the swiftness with which mitigation is reduced. Note that as $t \to \infty$, $m(t) \to 0$.

More generally, the complete characterization of the optimal policy path is the solution to an optimal control problem. We formally state that problem in Appendix A. It shows that the key trade-off with mitigation efforts $m$ is that a marginal increase in $m$ entails static economic...
costs of $W_m(x, m)$ stemming from the loss of output and thus consumption of all individuals in the economy, as encoded in $y = y(m)$. The dynamic benefit is a favorable change in the population health distribution: an increase in $m$ reduces the outflow of individuals from the susceptible to the asymptomatic state.

4 Calibration

Our calibration procedure has two parts. The first involves selecting a large set of parameter values in a standard way based on a mix of external evidence and choices about empirical counterparts to model objects. The second part is more delicate, and has to do with quantifying the aggregate evolution of the pandemic in its early stages. In this second step we need to estimate changes in behavior and policies as the United States moved from business-as-usual to a partial lock-down coupled with a set of behavioral changes designed to reduce the spread of infection. We begin with the first, and more straightforward, part of the calibration.

We set the population share of the young, $\mu^y$, to be 85%, which is the current fraction of the US population below the age of 65.

Preferences We assume logarithmic utility from consumption:

$$u(c) = \log c.$$ 

We set the pure time discount rate in annual terms to 3%. To accommodate differential mortality by age in the simplest way we assume that 500 days after the start of the pandemic (sufficient for it to have run its course), the discount rate becomes 4% for the young and 10% for the old. These values are chosen to reflect, respectively, a residual expected duration of life of 47.5 years for a 32.5 year old, and of 14 years for a 72.5 year old, numbers which are consistent with recent pre-COVID-19 life tables.

To set the value of life $\bar{u}$, we follow the value of a statistical life (VSL) approach. The Environmental Protection Agency and the Department of Transportation assume a VSL of $11.5$ million (see Greenstone and Nigam 2020). This is a high value, relative to values used in other contexts. Assuming an average of 37 residual life years discounted at a 3% rate, this translates into an annual flow value of $515,000$, which is 11.4 times yearly per capita consumption in the United States.
To translate this into a value for \( \bar{u} \) we use the standard value of a statistical life calculation,

\[
VSL = \frac{dc}{dr} \bigg|_{E[u]=k} = \frac{\ln(\bar{c}) + \bar{u}}{1 - r},
\]

where \( \bar{c} \) is average per capita model consumption, and \( r \) is the risk of death. Setting \( VSL = 11.4\bar{c} \) and \( r = 0 \) gives \( \bar{u} = 11.4 - \ln \bar{c} \). Note that this implies an easily interpretable trade-off between mortality risk and consumption. For example, we can ask what reduction in consumption leads to an individual becoming indifferent to facing a 1% risk of death. The answer is the solution \( m \) to

\[
\ln(\bar{c} (1 - m)) + 11.4 - \ln \bar{c} = 0.99 (\ln(\bar{c}) + 11.4 - \ln \bar{c}),
\]

which is \( m = 1 - \exp(-0.01 \times 11.4) = 10.8\% \).

As another way to get a feeling for what our choice for the value of a statistical life implies, suppose we were to contemplate a shut-down that would reduce consumption for six months by 25%. By how much would this shut-down have to reduce mortality risk for an agent with 10 expected years of life for the agent to prefer the shutdown to no shutdown? The answer is the solution \( x \) to

\[
\frac{1}{20} \ln(1 - 0.25) + \frac{19}{20} \ln(1) + 11.4 = (1 - x)11.4,
\]

which is 0.13%.

For the disutility of having flu, we define \( \hat{u}^f \) as

\[
\hat{u}^f = -0.3 (\ln(\bar{c}) + \bar{u}),
\]

following Hong et al. (2018). We set \( \hat{u}^e = -(\ln(\bar{c}) + \bar{u}) \), so that the flow value of being in hospital is equal to the flow value of being dead (zero).

**Sectors**

To calibrate the employment and output share of the basic sector of the economy, \( \mu^b \), we use BLS employment shares by industry. We categorize the following industries as basic: agriculture, health care, financial activities, utilities, and federal government. Mining, construction, manufacturing, education, and leisure and hospitality are allocated to the luxury sector. The remaining industries are assumed to be a representative mix of basic and luxury. This partition implies that pre-COVID, the basic sector accounts for \( \mu^b = 45.4\% \) of the
Redistribution We adopt the quadratic formulation of transfer costs described above. We pick a value for $\tau$ using estimates for the excess burden of taxation, which suggest that raising an extra dollar in revenue at the margin (which can be used to increase consumption for non-workers) has a cost for taxpayers of around $1.38 (Saez et al. 2012). This suggests $\frac{1-\nu}{\nu} c^n = 0.38$. Given the first order condition above, this means that an optimal redistribution scheme would imply $c_n/c_w = 1/1.38 = 0.72$ in pre-COVID times. Moreover, given $\eta \Theta = 0.021$, $\tau \frac{1-\nu}{\nu} c^n = 0.38$, and $\nu = \mu^y = 0.85$, section 3.2 implies $\tau = 3.51$.

Hospital Capacity Tsai et al. (2020) estimate that 58,000 ICU beds are potentially available nationwide to treat COVID-19 patients. However, only 21.5% of COVID-19 hospital admissions require intensive care, suggesting that total hospital capacity is around $58,000/0.215 = 270,000$. Tsai et al. (2020) emphasize that this capacity is very unevenly allocated geographically, and in addition, there is significant geographic variation in virus spread. Thus, capacity constraints are likely to bind in more and more locations as the virus spreads. We therefore set $\Theta = 100,000$, so that hospital mortality starts to rise when $0.042\%$ of the population is hospitalized. Because the cost of a day in intensive care is around $7,500, we set $\eta = 50$, so emergency care consumes about $2.1\%$ of pre-COVID output.\footnote{Total health care spending in the United States is $18\%$ of GDP. Of this, around one third is spending on hospitals.} We set the parameter $\lambda_o$ such that the death rate in emergency care for the old at the peak of the epidemic in our baseline calibration is $20\%$ above its value when capacity is not exceeded.\footnote{Much of the concern about exceeding capacity has focused on a potential shortage of ventilators. However, recent evidence from New York City indicates that $80\%$ of ventilated COVID-19 patients die, suggesting a limited maximum potential excess mortality rate associated with this particular channel.}

Disease Progression There are $12 \sigma$ parameters to calibrate, describing transition rates for disease progression, six for each age. These describe the chance of moving to the next worst health status and the chance of recovery at the three infectious stages: asymptomatic, flu-suffering, and hospitalized. We assume that young and old exit each stage at the same rate but potentially differ in the share of these exits that are into recovery. In particular, the old will be much more likely to require hospital care conditional on developing flu-like symptoms and more likely to die conditional on being hospitalized.

Putting aside these differences by age for a moment, the six values for $\sigma$ are identified
from the following six target moments: the average duration of time individuals spend in the asymptomatic (contagious but without symptoms for the disease.), flu-suffering (relatively mild symptoms), and emergency-care states, and the relative chance of recovery (relative to disease progression) in each of the three states. Following the literature on COVID-19 models, we set the three durations to 5.2, 10, and 8 days, respectively, with these durations common across age groups. The exit rate from the asymptomatic state to recovery defines the number of asymptomatic cases of COVID-19 and is an important but highly uncertain parameter. We assume that asymptomatic recovery and progression to the flu-suffering state are equally likely.\(^{14}\)

We let the relative rates of recovery from the flu-suffering and emergency care states vary with age, to reflect the fact that infections in older individuals are much more likely to require hospitalization and hospitalizations are also somewhat more likely to lead to death. We set the recovery rate from flu-suffering to 96\% for the young and 75\% for the old, based on evidence from Table 1 of the Imperial College study (Ferguson et al. 2020). Similarly, given evidence on differential mortality rates, we set the recovery rates from the emergency care state to 95\% for the young and 80\% for the old (assuming no hospital overuse). Given these choices, the probability that a newly infected young individual will ultimately die from COVID-19 is \(0.5 \times 0.04 \times 0.05 = 0.1\%\), while the conditional probability, conditional on developing flu symptoms, is 0.2\%. The corresponding numbers for an older individual are 2.5\% and 5.0\%.

**Sources of Infection**

Given the \(\sigma\) parameters, the parameters \(\alpha_w, \alpha_c, \beta_h, \) and \(\beta_e\) determine the rate at which contagion grows over time. We set \(\beta_e = 0.36\), implying that at the peak of infections, approximately 5\% of infections are to health care workers.\(^{15}\) The values of \(\alpha_w, \alpha_c, \) and \(\beta_h\) determine the overall basic reproduction number \(R_0\) value for COVID-19, and the share of disease transmission that occurs at work, via market consumption, and in non-market settings.

Mosssong et al. (2008) find that 35\% of potentially infectious inter-person contact happens in workplaces and schools, 19\% occurs in travel and leisure activities, and the remainder is in home and other settings.\(^{16}\) These shares should be interpreted as reflecting behaviors in

---

\(^{14}\)Given that the asymptomatic state has roughly half the duration of the flu state, this implies that roughly half of infected agents in the model will be asymptomatic. Recall that in a random sample in Iceland, half of the positive subjects reported no symptoms.

\(^{15}\)On March 24th, 14\% of Spain’s confirmed cases were health care workers. However, infection rates of health care workers appear lower in other countries. https://www.nytimes.com/2020/03/24/world/europe/coronavirus-europe-covid-19.html

\(^{16}\)Xu et al. (2020) discuss in detail heterogeneity in contact rates across different types of business (closed
a normal period of time, rather than in the midst of a pandemic. We associate workplace and school transmission with transmission at work, travel and leisure with consumption-related transmission, and the residual categories with transmission at home. These targets are used to pin down choices for $\alpha_w$ and $\alpha_c$, both relative to $\beta_h$, as follows.

The basic reproduction number $R_0$ is the number of people infected by a single asymptomatic person. For a single young person, assuming everyone else in the economy is susceptible and zero mitigation ($m = 0$), $R_{0y}$ is given by

$$R_{0y} = \frac{\alpha_w x y + \alpha_c \mu y + \beta_h}{\sigma y + \sigma y a f} + \frac{\sigma y a f}{\sigma y a f + \sigma y a r} \frac{\beta_h}{\sigma y a f + \sigma y a r} + \frac{\sigma y a f}{\sigma y a f + \sigma y a r} \frac{\sigma y f s}{\sigma y a f + \sigma y a r} \frac{\beta_e x y b}{\sigma e x y b}$$

where this expression exploits the fact that when $m = 0$, $\beta_w(0) = \alpha_w$ and $\beta_c(0) = \alpha_c$.

The logic is that this individual will spread the virus while asymptomatic, flu-suffering, and hospitalized—the three terms in the expression. They expect to be asymptomatic for $(\sigma y a r + \sigma y a f)^{-1}$ days, flu-suffering (conditional on reaching that state) for $(\sigma y f r + \sigma y f e)^{-1}$ days, and hospitalized (conditional on reaching that state) for $(\sigma y e r + \sigma y e d)^{-1}$ days. The chance they reach the flu-suffering state is $\sigma y a f / (\sigma y a f + \sigma y a r)$, and the chance they reach the emergency room is the product $\sigma y a f / (\sigma y a f + \sigma y a r) \sigma y f r / (\sigma y f r + \sigma y f e)$. While asymptomatic, they spread the virus both at work and at home, and pass the virus on to $\alpha_w x y + \alpha_c \mu y + \beta_h$ susceptible individuals per day. While flu-suffering, they stay at home and pass the virus to $\beta_h$ individuals per day. While sick they pass it to $\beta_e x y b$ basic workers per day in hospital.

The reproduction number for an old asymptomatic person is

$$R_{0o} = \frac{\alpha_c \mu y + \beta_h}{\sigma o a r + \sigma o a f} + \frac{\sigma o a f}{\sigma o a f + \sigma o a r} \frac{\beta_h}{\sigma o a f + \sigma o a r} + \frac{\sigma o a f}{\sigma o a f + \sigma o a r} \frac{\sigma o f s}{\sigma o a f + \sigma o a r} \frac{\beta_e x y b}{\sigma e x y b}$$

where this formula is similar to the one for the young, except that it recognizes that is less common for the old to pass the virus on, because they do not work. At the same time, however, because the old are less likely to recover once infected, they carry the virus for a potentially longer time, inducing more transmission in hospitals.

Recall that $x y$ is the pre-COVID number of workers, and $\alpha_w$ is the probability that transmission occurs when an infected worker meets a susceptible one. Recall that we assume consumption contagion is proportional to output, and pre-COVID output is $\mu y = x y$.17

office, open office, manufacturing and retail) and a range of interventions that can reduce those rates.

17Recall that $x y$ is the pre-COVID number of workers, and $\alpha_w$ is the probability that transmission occurs when an infected worker meets a susceptible one. Recall that we assume consumption contagion is proportional to output, and pre-COVID output is $\mu y = x y$.17
For the population as a whole, the overall $R_0$ is a weighted average of these two group-specific values

$$R_0 = \mu_y R_0^y + (1 - \mu_y) R_0^o,$$

where $\mu_y$ is the fraction of the population that is young.

In the workplace, the share of total transmission that occurs from a randomly drawn, newly asymptomatic individual is then given by

$$\frac{\text{workplace transmission}}{\text{all transmission}} = \frac{1}{R_0} \mu^y \left( \frac{\alpha_w}{\sigma^{yar} + \sigma^{yaf}} \right),$$

while the share of transmission due to market consumption is

$$\frac{\text{consumption transmission}}{\text{all transmission}} = \frac{1}{R_0} \left[ \mu^y \left( \frac{\mu^y \alpha_c}{\sigma^{yar} + \sigma^{yaf}} \right) + (1 - \mu^y) \left( \frac{\mu^y \alpha_c}{\sigma^{oar} + \sigma^{oaf}} \right) \right].$$

Given these three equations, we set the relative values $\alpha_w/\beta_h$, $\alpha_c/\beta_h$ to replicate shares of workplace and consumption transmission equal to 35% and 19%. Note that this evidence does not pin down the *levels* of $\alpha_w$, $\alpha_c$, and $\beta_h$, to which we now turn.

**History, $R_0$, and Initial Conditions**  We will think of a policy maker choosing a path for mitigation $m_t$ starting from April 12, 2020. The dynamics of the disease going forward, and thus the optimal path for $m_t$, will be highly sensitive to the distribution of the population by health status at this date: how many people of each type are susceptible, infected, and recovered; and how the infected group is partitioned by stage into asymptomatics, those with flu symptoms, and those in hospital. It is not easy to get an accurate cross-sectional picture of the health of the population, given that only a very small share of the population has recently been tested.

In addition, going forward, the dynamics of the disease will depend on the basic reproduction number $R_0$, which in our model is determined at a structural level by the levels of the infection-generating parameters $\alpha_w$, $\alpha_c$, and $\beta_h$. Existing estimates for $R_0$ for COVID-19, absent additional social distancing measures or economic shutdowns, are in the range of 2 to 4 (e.g., Flaxman et al. 2020). But given all the precautions that Americans are currently choosing to take or being required to take, the current effective $R_0$ is likely much lower. In addition, the
fact that a large share of the US economy has been shuttered has likely lowered $R_0$ still further.

To pin down the April 12 health status distribution and the April 12 level for the infection-generating parameters, we take the following approach. First, we will assume that America changed on March 21. Before that date, people behaved as normal, and none of the economy was shuttered, corresponding to $m = 0$. On March 21, we assume infection-generating rates fell discretely and proportionately to new lower levels $\zeta \alpha_w$, $\zeta \alpha_c$, and $\zeta \beta_h$ with $\zeta < 1$. In addition, and at the same date, we assume that states introduced measures that effectively shut down a fraction $m = 0.5$ of the luxury sector, therefore immediately idling $0.5(1 - \mu^b) = 27.5\%$ of the workforce. It is difficult to assess how much of economy has been affected directly or indirectly by shutdown measures, but our value for $m$ is consistent with the Faria-e-Castro (2020) forecast that US unemployment will rise above 30% in the second quarter (Bick and Blandin 2020 estimate that it is already 20%). Of course, in reality changes in social distancing practices and shutdowns happened more gradually, but March 21 seems a natural focal date: California announced the closure of non-essential businesses on March 19, and New York and Illinois did so on March 20.

Of the data we have on health outcomes, perhaps the most reliable are for the number of deaths attributable to COVID-19. We will therefore target three specific moments involving deaths: the cumulative number of deaths up to March 21 (301), the cumulative number as of April 12 (22,100), and the moving-average number of deaths per day by April 12 (2,000). To hit these target moments, we treat as free parameters (1) $\beta_h$ — the pre-March 21 infection-generating rate at home; (2) $\zeta$, the proportional amount by which infection-generating rates fall on March 21; and (3) the initial number of infections at the date we start our model simulation, which is February 12.

Table 1: Millions of People in Each Health State

<table>
<thead>
<tr>
<th></th>
<th>$S$</th>
<th>$A$</th>
<th>$F$</th>
<th>$E$</th>
<th>$R$</th>
</tr>
</thead>
<tbody>
<tr>
<td>March 21</td>
<td>321.84</td>
<td>5.57</td>
<td>1.04</td>
<td>0.01</td>
<td>1.54</td>
</tr>
<tr>
<td>April 12</td>
<td>305.39</td>
<td>4.16</td>
<td>3.68</td>
<td>0.15</td>
<td>16.59</td>
</tr>
</tbody>
</table>

To understand how this identification scheme works, consider that the death toll rose from 301 to 22,100 deaths in only three weeks, but the number of daily deaths was not especially high (nor was it growing especially fast) at the end of this period. This suggests that there
were already many infections in the pipeline on March 21, but those infections did not grow rapidly from March 21 onward, which indicates a low value for $\zeta$. At the same time, a high level of March 21 infections is informative about the level of initial infections on February 12. Finally, a large number of infections on March 21, but low death toll up to that date, points to high $R_0$ (and a high $\beta_h$) before March 21: rapid spread can deliver lots of new infections without many deaths (yet). This calibration strategy yields an initial effective $R_0$ before March 21 of 3.0, which falls to 0.72 after March 21, reflecting a value for $\zeta$ of 0.33. Part of this decline reflects the start of economic mitigation. Absent mitigation (with $m = 0$), the effective $R_0$ after March 21 would be 1.0. This calibration implies the distribution of the population by health status summarized in Table 1. Thus, the calibration implies that 2.0% of the US population was actively infected on March 21, with that number rising to 2.4% by April 12.

Table 2: Epidemiological Parameter Values

<table>
<thead>
<tr>
<th>Behavior-Contagion (before March 21)</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha_w$ infection at work</td>
<td>35% of infections</td>
</tr>
<tr>
<td>$\alpha_c$ infection through consumption</td>
<td>19% of infections</td>
</tr>
<tr>
<td>$\beta_h$ infection at home</td>
<td>$R_0 = 3.0$</td>
</tr>
<tr>
<td>$\beta_e$ infection in hospitals</td>
<td>5% of infections at peak</td>
</tr>
<tr>
<td>$\zeta$ scale of social distancing</td>
<td>$R_0 = 1.0 w/ m = 0$</td>
</tr>
</tbody>
</table>

Disease Evolution

<table>
<thead>
<tr>
<th>Rate Description</th>
<th>Rate</th>
<th>Days</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma^{yaf}$ rate for young asymptomatic into flu</td>
<td>50% flu, 5.2 days</td>
<td>0.5</td>
<td></td>
</tr>
<tr>
<td>$\sigma^{var}$ rate for young asymptomatic into recovered</td>
<td>0.3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma^{oaf}$ rate for old asymptomatic into flu</td>
<td>50% flu, 5.2 days</td>
<td>0.3</td>
<td></td>
</tr>
<tr>
<td>$\sigma^{lar}$ rate for old asymptomatic into recovered</td>
<td>0.3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma^{yfe}$ rate for young flu into emergency</td>
<td>4% hospitalization, 10 days</td>
<td>0.04</td>
<td></td>
</tr>
<tr>
<td>$\sigma^{yfr}$ rate for young flu into recovered</td>
<td>0.06</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma^{ofe}$ rate for old flu into emergency</td>
<td>25% hospitalization, 10 days</td>
<td>0.25</td>
<td></td>
</tr>
<tr>
<td>$\sigma^{ofr}$ rate for old flu into recovered</td>
<td>0.25</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma^{ved}$ rate for young emergency into dead</td>
<td>0.2% mortality, 8 days</td>
<td>0.05</td>
<td></td>
</tr>
<tr>
<td>$\sigma^{ver}$ rate for young emergency into recovered</td>
<td>0.8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma^{oed}$ rate for old emergency into dead</td>
<td>5.0% mortality, 8 days</td>
<td>0.20</td>
<td></td>
</tr>
<tr>
<td>$\sigma^{oer}$ rate for old emergency into recovered</td>
<td>0.8</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
with an additional 5.1% having recovered.\footnote{These numbers are within the range of expert estimates from the COVID-19 survey compiled by McAndrew (2020) at the University of Massachusetts.}

For the time path of mitigation, our baseline simulation, designed to approximate current US policy, will assume $m = 0.5$ for 100 days from March 21 onward, followed by $m = 0$ thereafter. This path is implemented in the context of the mitigation function (eq. 44) by setting $\gamma_0 = 0.5$, $\gamma_1 = -0.3$, and $\gamma_2 = 100$.

Table 3: Economic Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\rho_y$</td>
<td>effective discount rate of young</td>
<td>0.04% per year</td>
</tr>
<tr>
<td>$\rho_o$</td>
<td>effective discount rate of old</td>
<td>0.10% per year</td>
</tr>
<tr>
<td>$\bar{u}$</td>
<td>value of life</td>
<td>11.4x consumption p.c.</td>
</tr>
<tr>
<td>$\bar{u}^f$</td>
<td>disutility of flu</td>
<td>lose 30% of baseline utility</td>
</tr>
<tr>
<td>$\bar{u}^e$</td>
<td>disutility of emergency care</td>
<td>lose 100% of baseline utility</td>
</tr>
<tr>
<td>$\mu^b$</td>
<td>size of basic sector</td>
<td>45.4%</td>
</tr>
<tr>
<td>$\mu^y$</td>
<td>share of young</td>
<td>85%</td>
</tr>
<tr>
<td>$\tau$</td>
<td>transfer cost</td>
<td>$0.38 burden of excess taxation</td>
</tr>
<tr>
<td>$\alpha_0$</td>
<td>initial share mitigated</td>
<td>50%</td>
</tr>
<tr>
<td>$\alpha_1$</td>
<td>speed of mitigation</td>
<td>-0.3</td>
</tr>
<tr>
<td>$\alpha_2$</td>
<td>time mitigation begins</td>
<td>100 days</td>
</tr>
<tr>
<td>$\Theta$</td>
<td>hospital capacity</td>
<td>100,000 beds</td>
</tr>
<tr>
<td>$\eta$</td>
<td>bed cost</td>
<td>$7,500</td>
</tr>
<tr>
<td>$\lambda_o$</td>
<td>impact of overuse on mortality</td>
<td>20% higher mortality at peak</td>
</tr>
</tbody>
</table>

5 Findings

We start by describing model outcomes under what we think of as the policies currently in place in the United States. We then turn in the next section to optimal mitigation.

5.1 Benchmark Results

In Figures 1 to 5, we display the population health dynamics from March 21 to the end of 2020. The red dashed lines represent our baseline scenario with 50% economic mitigation.
\( m_t = 0.5 \) for 100 days and social distancing as described in Section 4. The blue solid line is an alternative that shares the same time path of parameters and policies before April 12 – including 50% mitigation between March 21 and April 12 – but in which mitigation is set to zero from April 12 onward.

![Diagram of infection rates](image)

**Figure 1:** Share of Each Group Infected (Asymptomatic + Flu + Hospitalized).

We start with the currently infected (asymptomatic plus those with flu symptoms and those in hospital) in Figure 1. Under our baseline policy, the red dashed line indicates that on April 12, we are already close to the peak of active infections. In contrast, if economic mitigation were to cease being enforced starting on April 12, the share of the population actively infected would nearly triple instead, reaching around 5.5% of the population at the end of May. With economic mitigation continuing into June, that share never exceeds 2.5% of the population. The figure also shows that the timing of the relaxation of economic mitigation matters greatly: in the benchmark, the partial shutdown is lifted at the end of June, and although infections increase mildly over the next two months, the peak infection rates are never nearly as large as
under the scenario when economic mitigation ends now (April 12).

![Graphs showing the share of each group infected but asymptomatic over time with different levels of economic mitigation.]

**Figure 2: Share of Each Group Infected but Asymptomatic**

Turning to the heterogeneity across the population, note that absent economic mitigation, basic and luxury sector workers are infected at nearly identical rates, while the old – who do not face exposure at work – experience a much lower rate of infection. Economic mitigation reduces infection rates for all three types. Comparing the two types of workers, the effect of mitigation (i.e., the gap between the blue solid and the red dashed line) is slightly larger for luxury workers – since a share of them stays at home under economic mitigation. But all three groups benefit from economic mitigation to a surprisingly similar extent, reflecting the fact that lower virus spread at work means fewer infected people outside of work and thus fewer new infections at home and in stores.

The next three figures decompose active infections into the asymptomatic (Figure 2), those suffering from flu-like symptoms (Figure 3), and those in hospital (4). The key observation to
Figure 3: Share of Each Group with Flu Symptoms
note here is that while a smaller share of the old develops mild symptoms, reflecting a lower infection rate (see Figure 3), a much larger share of the old population ends up being severely sick and hospitalized, as the lower right panel of Figure 4 shows. This is true under both mitigation scenarios, but the effect is especially pronounced if economic mitigation is abolished early: infections skyrocket first in the workplace and then at home and during shopping trips, translating into more infections among the old. Although the old are only half as likely as the young to become infected, conditional on becoming infected they are over six times as likely to eventually require hospitalization.

![Figure 4: Share of Each Group Hospitalized.](image)

The red horizontal line in the upper left panel of Figure 4 plots hospital capacity, $\Theta$, which we assume to be fixed in the short run. This plot shows another dramatic difference between the two mitigation scenarios. Under the benchmark scenario with 50% economic mitigation until the end of June, the demand for hospital care almost never exceeds capacity, with a modest exception in the weeks of April. However, even then, excess demand is never severe, and thus the excess death rate that comes with overstretched hospitals is mild and short-lived.
Contrast this to the (counterfactual) scenario when economic mitigation policies are suspended on April 12. The blue line in the upper left panel of Figure 4 indicates that capacity is drastically exceeded for several months in this scenario.

Figure 5 shows daily deaths from COVID-19. Under the baseline policy, with 50% mitigation, deaths rise a little but never exceed 2,500 per day. If economic mitigation ends at Easter, the daily death toll rises dramatically, exceeding 6,000 at the peak. The breakdown across population groups indicates that the virus is predicted to kill more older individuals than younger ones, even though the old account for only 15% of the population.

A useful test of the model is to compare model-predicted mortality by age to the data that is available to date. In the model, the old account for 67% of cumulative deaths up to April 12. By comparison, of the 6,839 deaths reported in New York City as of April 14, 72.3% were associated with individuals over 65. Thus, the age variation that arises in the model in infection and disease progression probabilities is broadly consistent with the observed age distribution of mortality.
Figure 6: Left Panel: Share of the Initial Population Deceased. Right Panel: Share of Population Never Infected (Susceptible).
In Figure 6 we display the population health dynamics over the next 18 months under three different scenarios, starting on April 12. The red dashed line represents the baseline scenario with 50% economic mitigation for 100 days. The solid blue scenario is again the case with no work mitigation. The new cyan dashed line describes the population dynamics associated with the Optimal Work Mitigation path discussed in detail in Section 5.2. The left panel displays the cumulative share of the population that has died from the virus, and the right panel plots, against time, the share of the population that has not yet been infected (i.e., the susceptible group).

Absent economic mitigation, the virus spreads rapidly, and after about three months, 50% of the U.S. population has been (or is currently) infected with the virus: the blue line with the never-infected share of the population rapidly drops below 50%. In contrast, under our projection for the current economic mitigation plan, the never-infected share declines more slowly, and a significantly larger share of the population is never touched by the virus (60% rather than 50%). That is, aggressive mitigation measures do not just flatten the curve: they also reduce the total number of infections. The logic is that in the SIR class of models, the growth rate of infections depends not just on how many people are infected but also on the relative shares of susceptible versus recovered individuals in the non-infected population. More aggressive mitigation measures slow the spread of infection, such that infections peak later. But delaying the peak in infections gives time for more people to recover and develop immunity, which slows infection growth. The result is that the economy converges to a steady state in which a larger share of individuals has never been infected, relative to the scenario in which the economy open up at Easter.

The left panel translates infections into mortality associated with the virus. In the absence of economic mitigation, the death toll of the virus rises rapidly, and by the end of the outbreak 0.18% of the U.S. population is predicted to have lost their lives, which amounts to 590,000 people. Under the current benchmark economic mitigation policy, that number falls to 0.1275% (418,000 individuals). The difference in lives lost (172,000) comes from two sources. First, with economic mitigation in place, there is less hospital overload and excess associated mortality. Second, with mitigation, a smaller cumulative total number of infections means that fewer people ever risk adverse health outcomes and death. Of the 590,000 total death toll absent any economic mitigation from April 12 onward, 120,000 deaths are due to hospital capacity being exceeded. Under the baseline 50-percent-for-100-days mitigation policy, only 3,000 out of 418,000 deaths reflect hospital overload. Thus, 117,000 of the extra 172,000 lives lost
when the shutdown ends at Easter reflect a severely over-stretched hospital system.

Finally, the figure also anticipates our optimal-mitigation policy finding that the optimal mitigation path is somewhere between the current level of economic shutdown and no shutdown at all, with health consequences that lie between the benchmark and the no-economic-mitigation scenario. We will discuss this finding in greater detail in the next section.

Figure 7 plots the dynamics of consumption for workers, and non-workers through the course of the pandemic. Recall that in this economy, all workers independent of sector, enjoy the same consumption level, and the government provides equal consumption via transfers to all non-workers, irrespective of whether they are not working because they are old, sick, or asked to stay home because of economic mitigation. The four panels correspond to four different economies. In the top two panels, we assume our baseline value for $\tau$, which implies that it is costly for the planner to redistribute from workers to non-workers. In the bottom two panels, we set $\tau = 0$, so that the planner can freely redistribute. In that case, the planner equates consumption between workers and non-workers at each date.\footnote{Recall that the evolution of the population health distribution is independent of the cost of transfers.}

Comparing across columns, the left two panels display the evolution of consumption when economic mitigation ends on April 12, and the right two panels maintain 50% mitigation until the end of June. In the first case, the economy immediately recovers as all healthy workers who were affected by the shutdown in the luxury sector return to work, increasing output, income, and thus aggregate consumption in the economy by about 27.5%.\footnote{Note that we assume that infected people with symptoms stay home rather than go to work, and since the share of infected individuals is endogenously evolving over time, the increase is not exactly equal to the 27.5% decline in output when economic mitigation was introduced in the first place.} The right two panels show that in terms of output and thus consumption, a later end to the shutdown simply (and somewhat mechanically) postpones the economic recovery by 2.5 months. Note from the upper right panel of Figure 7 that the cost of economic mitigation is borne disproportionately by non-workers: the ratio of non-worker to worker consumption declines (from two-thirds to one-half) during the mitigation phase. This reflects our assumption that extracting resources to redistribute from workers becomes ever harder the more the planner wants to tax each worker. To avoid very large redistribution costs, the planner optimally chooses to reduce insurance during the mitigation phase and increases it again as the economy recovers.

Next, we report the expected welfare gains and losses for each type of individual for various...
Figure 7: Consumption Paths. Top Two Panels, $\tau = 3.51$. Bottom Two Panels, $\tau = 0$. Left Two Panels, $m = 0$. Right Two Panels, $m = 0.5$ for 100 Days, Then $m = 0$. 
Table 4: Welfare Gains (+) or Losses (-) From Mitigation

<table>
<thead>
<tr>
<th>Mitigated Share</th>
<th>50%</th>
<th>25%</th>
<th>10%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Young Basic</td>
<td>-0.01%</td>
<td>-0.08%</td>
<td>0.10%</td>
</tr>
<tr>
<td>Young Luxury</td>
<td>-0.31%</td>
<td>-0.08%</td>
<td>-0.03%</td>
</tr>
<tr>
<td>Old</td>
<td>1.18%</td>
<td>1.72%</td>
<td>1.32%</td>
</tr>
</tbody>
</table>

assumptions about the level of economic mitigation and the parameter $\tau$ that indexes the cost of redistribution. In particular, we consider three mitigation levels: $m = 0.5$ (our baseline used to construct the previous plots), $m = 0.25$, and $m = 0.1$. In each case, we assume mitigation is in place for 100 days from March 21. The welfare calculation asks, What% of consumption would a person be willing to pay every day for the rest of his life to move from the economy with $m = 0$ to the one with $m = 0.5$ (or $m = 0.25$ or $m = 0.1$) for 100 days? We report results for our baseline value for $\tau$ (3.51) and for a case in which redistribution is costless ($\tau = 0$).

The first clear message from Table 4 is that economic mitigation offers significant welfare gains for the old but has much more modest welfare effects on the young. For example, in our baseline case ($m = 0.5$ and $\tau = 3.51$), the old gain 1.18% of consumption, while the young basic workers are essentially indifferent relative to no shutdown, and young luxury workers experience welfare losses equivalent to losing 0.31% of consumption. The reason the gains are much larger for the old is simply that the old face a much higher likelihood of being killed by the virus, and strong economic mitigation policies reduce infections in the workplace, which in turn lowers the risk that the old meet infected individuals at home or while shopping.

The second key message is that the cost of redistribution matters. In particular, when redistribution is costless, young luxury workers and young basic workers perceive essentially identical welfare effects from mitigation.\textsuperscript{21} However, when redistribution is costly, young luxury workers fare notably worse than young basic workers because they risk larger expected consumption losses from economic mitigation. The reason is that when mitigation is increased, the planner needs to redistribute from a smaller pool of workers toward a larger pool of non-workers. Given convex costs of extracting additional resources from workers, this induces the planner to reduce insurance, translating into a larger consumption gap between workers and non-workers.

\textsuperscript{21}In fact, luxury workers are slightly more pro-mitigation, since they benefit more from reduced infection at work.
We now briefly discuss a few factors that shape these welfare calculations. First, the overall level of the welfare numbers is sensitive to several choices. A key one is the value of a statistical life: a lower value would make life-saving economic mitigation trivially less attractive. Second, if we assumed lower recovery rates at different stages of an infection, or a higher mortality rate at the hospital stage, agents would perceive a greater risk of death and be more willing to sacrifice consumption to avoid that risk. Third, in our model, when a shutdown raises non-employment and reduces consumption, there is no upside in households’ utility functions from more leisure. In the analysis of optimal shutdowns in Eichenbaum et al. (2020), the fact that households experience reduced disutility from labor supply when economic activity is taxed compensates strongly for the utility cost of reduced consumption. Fourth, if we were to make outputs of the basic and luxury sectors imperfect substitutes, then reducing luxury sector output would have a larger negative impact on aggregate consumption, and shutdowns would be less appealing. Fifth, if business failures caused by the shutdown lead to the destruction of firm-specific capital, then the shutdown will continue to depress output even after it is lifted, again suggesting a softer optimal shutdown. Finally, the attractiveness of shutdowns clearly depends on the share of virus transmission that occurs through different forms of economic activity: the larger that share is, the more powerful shutdowns are as a tool to slow transmission.

5.2 Optimal Policy

The mitigation policies we have compared thus far were not chosen optimally. We now turn to exploring the optimal time path for economic mitigation and the associated statically optimal degree of redistribution, given that path. To start, we optimize over the three parameters in our parametric process for \( m_t \). That is, we choose \( \gamma_0 \), \( \gamma_1 \), and \( \gamma_2 \) in eq. 44 to maximize social welfare as defined in Section 3.2. The choice of these parameters lets the government control the initial size of economic mitigation, when it ends, and how quickly it is phased out. Figure 8 describes the preferred policies within this class.

The left panel describes optimal policies under our baseline cost for redistribution, with \( \tau = 3.51 \). The blue line is the policy chosen by a utilitarian planner, who weighs the expected utility of each type in proportion to its date 0 population shares. The other lines describe the policies preferred by each of the three different types (young workers in the basic sector, young workers in the luxury sector, and old individuals, respectively). The right panel corresponds to a case in which redistribution to soften the economic effects of mitigation is costless (\( \tau = 0 \)).
Figure 8: Preferred Intensity and Duration of Lockdowns
There are clearly large differences across individual types in terms of what fraction of the economy they would like to see shut down and for how long. As a point of comparison, recall that up until April 12, the level of mitigation is set at 50% of the luxury sector. We first focus on the benchmark calibration with costly transfers (the left panel).

The old (15% of the population) would like to see about 35% of the luxury sector shut down for about 110 days, before the shutdown is slowly lifted, and completely wound down by November 2020. In contrast, young luxury workers (close to 50% of the entire population) would prefer a much lower level of mitigation and for that mitigation to end much earlier. Basic sector workers have a policy preference roughly in the middle of these two extremes, and a utilitarian government adopts a similar policy. Thus, a utilitarian government closes about 25% of the luxury sector until around the end of June, before gradually opening up over the following month. Note that this policy implies a notably lower level of economic mitigation than the one currently in place. At the same time, some mitigation is certainly called for, and our model suggests it should remain in place for an extended period of time.

When redistribution is costless (right panel of Figure 8), policy preferences remain qualitatively similar but quantitatively change quite significantly. First, young workers in both sectors now broadly agree on the preferred mitigation policy, which is not surprising since they face identical consumption consequences. Second, the old now prefer even more mitigation, because they do not have to worry about a reduction in relative consumption during a shutdown. The utilitarian policy is more aligned with the preferences of young workers, simply because they constitute the lion’s share of the population. Interestingly, the preferred utilitarian mitigation policy is more aggressive when redistribution is (counter-factually) costless, both in terms of level as well as in terms of a longer and more gradual phasing-out. However, even when redistribution is costless, the optimal level of economic mitigation is still below the level we believe to be currently in place.

The next two tables (Tables 5 and 6) describe expected welfare gains, relative to a no-economic-mitigation baseline, under each of the policies described in Figure 8. The columns of each table identify the policy in place. The rows report expected welfare for each type.

Consistent with the results in the previous section, the old experience large welfare gains from any of these policies. Irrespective of the cost of redistribution, the welfare gains or losses for the young are much smaller. Second, and again in line with the previous section, the welfare gains
Table 5: Welfare Gains (+) or Losses (-) From Preferred Mitigation, $\tau = 3.51$

<table>
<thead>
<tr>
<th></th>
<th>Utilitarian</th>
<th>Old</th>
<th>Young Luxury</th>
<th>Young Basic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Young Basic</td>
<td>0.10%</td>
<td>0.03%</td>
<td>0.08%</td>
<td>0.10%</td>
</tr>
<tr>
<td>Young Luxury</td>
<td>0.02%</td>
<td>-0.23%</td>
<td>0.04%</td>
<td>0.01%</td>
</tr>
<tr>
<td>Old</td>
<td>1.15%</td>
<td>1.54%</td>
<td>0.74%</td>
<td>1.18%</td>
</tr>
</tbody>
</table>

Table 6: Welfare Gains (+) or Losses (-) From Preferred Mitigation, $\tau = 0$

<table>
<thead>
<tr>
<th></th>
<th>Utilitarian</th>
<th>Old</th>
<th>Young Luxury</th>
<th>Young Basic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Young Basic</td>
<td>0.06%</td>
<td>-0.17%</td>
<td>0.07%</td>
<td>0.07%</td>
</tr>
<tr>
<td>Young Luxury</td>
<td>0.07%</td>
<td>-0.17%</td>
<td>0.08%</td>
<td>0.08%</td>
</tr>
<tr>
<td>Old</td>
<td>1.66%</td>
<td>2.27%</td>
<td>1.31%</td>
<td>1.26%</td>
</tr>
</tbody>
</table>

for young luxury workers are always smaller than for young basic workers when redistribution is costly, while the pattern is reversed when redistribution is costless. Third, when redistribution is costly, the policy that is welfare maximizing for the old is actually welfare-reducing (relative to no mitigation) for young luxury workers.

6 Conclusion

We built a model in which the distributions of economic activity and health are jointly determined. Individuals in the model are heterogeneous by age, sector, and health status. We model multiple sources of disease transmission, and how this transmission affects and is affected by the level of economic activity. We studied optimal economic mitigation policies and argued that costly redistribution reduces the desire of the government to engage in such policies. Our results also starkly illustrate how unevenly the welfare gains and losses from economic mitigation are likely distributed across different segments of society. The elderly gain much more than the young from extensive reductions in economic activity than the young. Those working in the partially shuttered sector are the most adversely impacted, especially when it is costly to soften the distributional consequences via public transfers. Our baseline calibration suggests that the shutdown in place on April 12 was too extensive, but that a utilitarian planner would keep a partial shutdown in place through July.
References


Ferguson, N. M. et al. (2020): “Impact of non-pharmaceutical interventions (NPIs) to reduce COVID-19 mortality and healthcare demand,” Imperial College COVID-19 Response Team.


A The Unrestricted Optimal Policy Problem

The complete characterization of the optimal policy path is the solution to an optimal control problem. In the main text we already have derived the period return function \( W(x, m) \). In addition, the evolution of the state (the distribution of the population by health status \( x = (x^{i,j}) \)) evolves according to the vector-valued equation (summarizing Equations (4) to (22) the paper in a compact form):

\[
\dot{x} = G(x, m) \tag{45}
\]

To solve for the optimal time path of the scalar mitigation variable is then a straightforward optimal control problem with a multi-dimensional state vector and a one-dimensional control variable. Define the current value Hamiltonian as

\[
\mathcal{H}(x, m, \mu) = W(x, m) + \mu G(x, m) \tag{46}
\]

where \( \mu \) is the vector of co-state variables associated with the population state vector \( x \). Necessary conditions at an interior solution for mitigation \( m \) are the optimality condition for \( m \)

\[
W_m(x, m) = -\mu \cdot G_m(x, m) \tag{47}
\]

\[
\dot{\mu} = \rho \mu - [W_x(x, m) + \mu \cdot G_x(x, m)] \tag{48}
\]

\[
\dot{x} = G(x, m) \tag{49}
\]

The key trade offs with mitigation efforts \( m \) discussed in the main text are encoded in equation (47). A marginal increase in \( m \) entails static economic costs of \( W_m(x, m) \) stemming from the loss of output and thus consumption of all individuals in the economy, as encoded in \( y^\alpha(m) \). The dynamic benefit is a better change in the population health distribution, as encoded in the vector \( G_m(x, m) \). Concretely, as is clear from equations (4 – 6) an increase in \( m \) reduces the outflow of individuals from the susceptible to the asymptomatic state. The value (in units of the objective function) are given by the co-state vector \( \mu \).

It should be kept in mind that since \( (x, \mu) \) are vectors, so are the entities \( G_m(x, m) = (G_{m}^{i,j}(x, m)) \) and \( W_x(x, m) = (W_{x}^{i,j}(x, m)) \) and \( G_x(x, m) = (G_{x}^{i,j}(x, m)) \) so that equation (47) reads explicitly

\[
W_m(x, m) = -\sum_{i,j} \mu^{i,j} G_{m}^{i,j}(x, m), \tag{50}
\]

and a specific row of the vector-valued equation (48) is given by

\[
\dot{\mu}^{i,j} = \rho \mu^{i,j} - \left[ W_{x}^{i,j}(x, m) + \sum_{k} \mu^{k} G_{x}^{k}(x, m) \right]. \tag{51}
\]